



Majority is not Enough: Bitcoin Mining is Vulnerable

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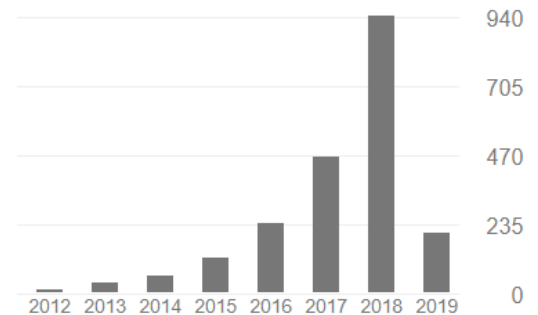
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Cryptocurrencies

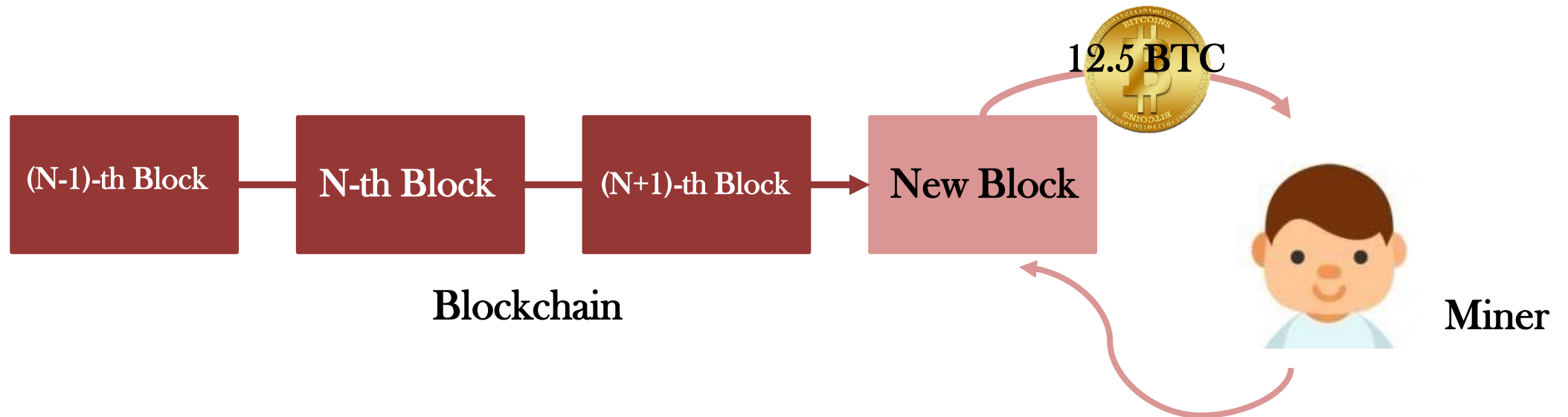


Popular algorithm: PoW

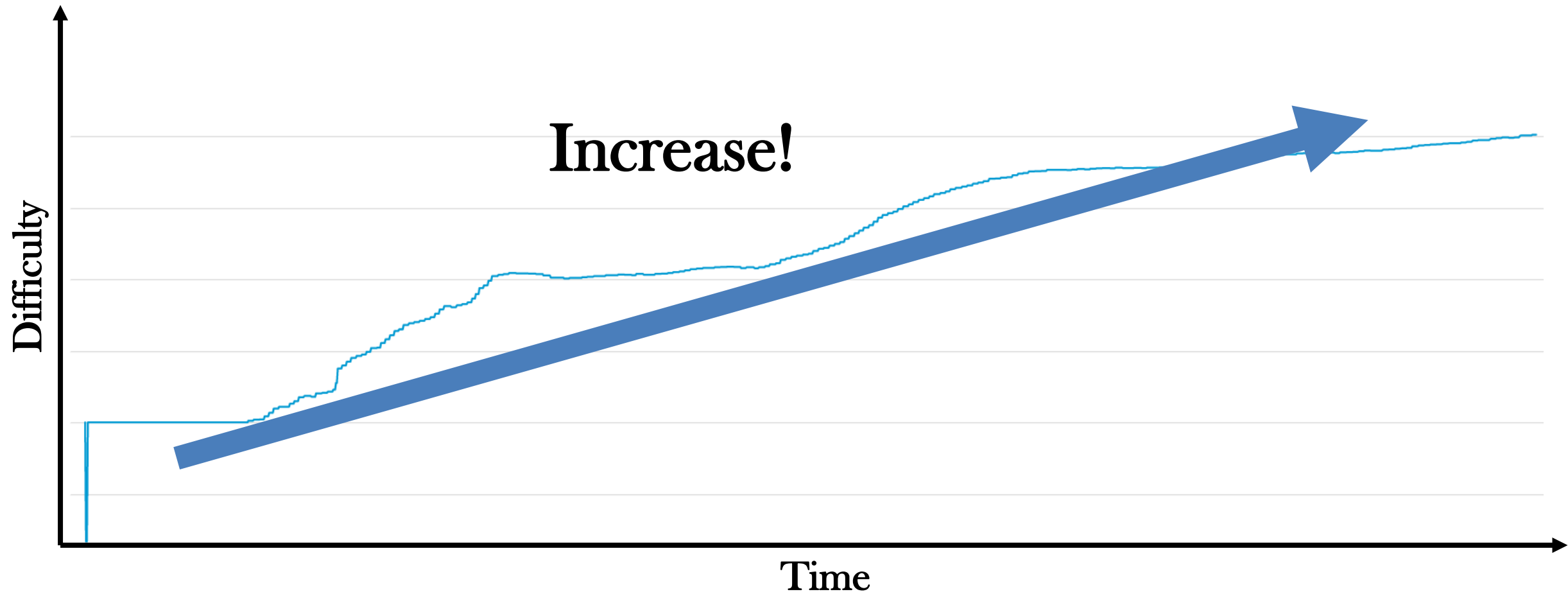
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#	Name	Market Cap	Price	Volume (24h)	Circulating Supply	Change (24h)	Price Graph (7d)		
1	 Bitcoin	\$70,773,218,524	\$4,019.46	\$8,915,802,711	17,607,650 BTC	-0.20%			...
2	 Ethereum	\$14,454,763,321	\$137.18	\$4,053,904,645	105,370,652 ETH	-0.43%			...
3	 XRP	\$12,895,478,801	\$0.309496	\$600,330,476	41,666,017,553 XRP *	-0.69%			...
4	 Litecoin	\$3,655,861,447	\$59.91	\$2,101,490,815	61,026,011 LTC	-1.82%			...
5	 EOS	\$3,303,811,081	\$3.65	\$1,388,966,728	906,245,118 EOS *	-0.69%			...
6	 Bitcoin Cash	\$2,919,181,847	\$165.02	\$411,585,974	17,690,000 BCH	0.06%			...
7	 Stellar	\$2,052,666,388	\$0.106769	\$193,767,980	19,225,307,919 XLM *	-1.27%			...
8	 Cardano	\$1,592,024,770	\$0.061404	\$112,386,088	25,927,070,538 ADA	-1.42%			...
9	 TRON	\$1,578,286,194	\$0.023669	\$305,340,812	66,682,072,191 TRX	-1.45%			...
10	 Bitcoin SV	\$1,170,414,897	\$66.24	\$80,843,318	17,670,348 BSV	-0.95%			...

Proof-of-Work Mining

- ❖ They use **blockchain** to run without a trusted third party.
- ❖ Miners generate blocks by spending their **computational power**.
- ❖ If a miner generates a valid block, he earns **reward** for the block.
- ❖ This process is **competitive**.



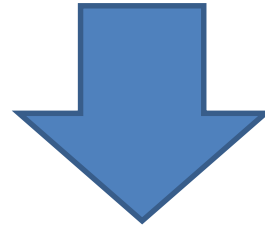
Mining Difficulty



From “<https://blockchain.info>”

Can we earn the extra reward through fork?

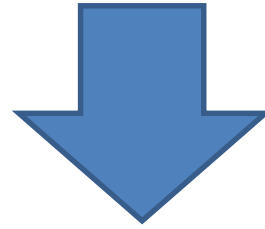
❖ The change of mining difficulty



❖ Validators consider the expected relative revenue per one round (10 mins) as their payoff.

Can we earn the extra reward through fork?

❖ The change of mining difficulty

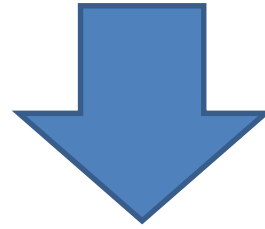


❖ Validators consider the expected relative revenue per one round (10 mins) as their payoff.

If a miner possesses 10% of the total computational power?

Can we earn the extra reward through fork?

❖ The change of mining difficulty



❖ Validators consider the expected relative revenue per one round (10 mins) as their payoff.

If a miner possesses 10% of the total computational power?

He earns 10% of the total reward.

Poisson distribution

- ❖ The Poisson distribution expresses the probability of a given number of events occurring in a fixed interval of time or space if these events occur with a known constant rate and *independently* of the time since the last event.

$$\text{Pr}[k \text{ events in one interval}] = e^{-\lambda} \frac{\lambda^k}{k!}$$

Poisson distribution

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$$\text{Pr}[k \text{ events in one interval}] = e^{-\lambda} \frac{\lambda^k}{k!}$$

In the **Bitcoin** system, one event means a generation of one block.



The 51% Attack

51% Attack

- ❖ Majority of hashing power has voted for transactions on longest chain.
 - It is costly to increase voting power
 - Players are not motivated to cheat
- ❖ If any party controls majority of hashing power, they can:
 - Undo the past
 - Deny mining rewards
 - Undermine the currency

Goldfinger Attack

- ❖ In the James Bond movie....
- ❖ The attacker's goal is to destroy Bitcoin by executing the 51% attack.
- ❖ Is a realistic attack?

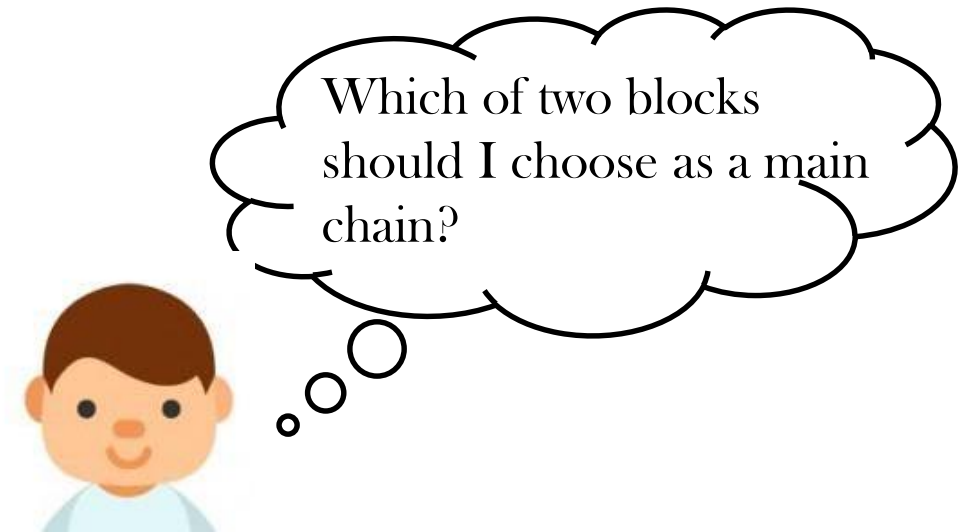
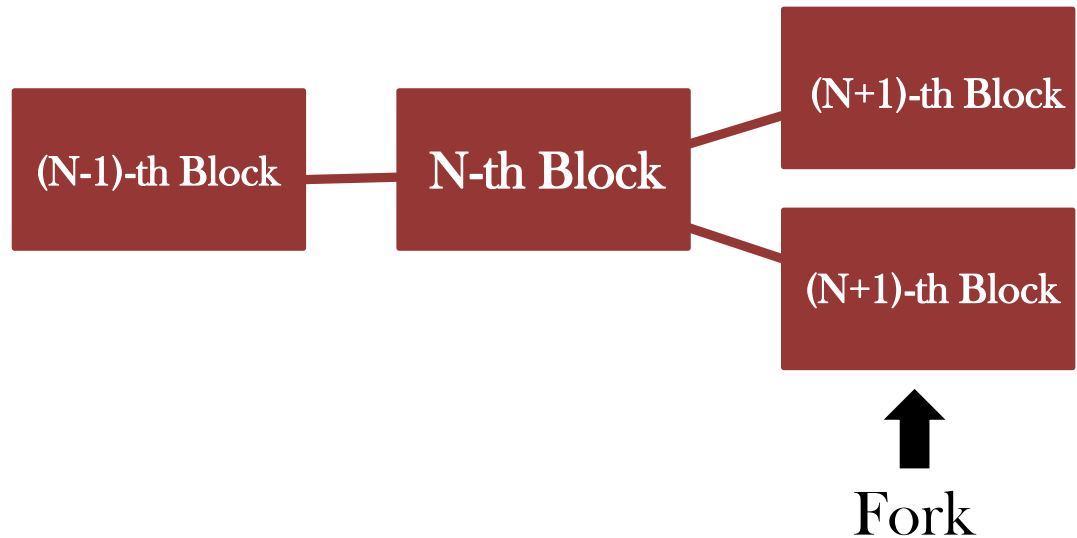


Selfish Mining

Selfish Mining

❖ Forks

- Due to the nonzero block propagation delay, nodes can have different views.
- When a fork occurs, only one block becomes valid.



Selfish Mining

- ❖ Generate intentional forks adaptively.
 - An attacker finds a valid block and propagates the block **when another block is found by an honest node.**
- ❖ Force the honest miners into wasting victims' computations on the stale public branch.

Strategy

```
6 on My pool found a block
7    $\Delta_{prev} \leftarrow \text{length}(\text{private chain}) - \text{length}(\text{public chain})$ 
8   append new block to private chain
9    $\text{privateBranchLen} \leftarrow \text{privateBranchLen} + 1$ 
10  if  $\Delta_{prev} = 0$  and  $\text{privateBranchLen} = 2$  then
11    publish all of the private chain
12     $\text{privateBranchLen} \leftarrow 0$ 
13    Mine at the new head of the private chain.

14 on Others found a block
15    $\Delta_{prev} \leftarrow \text{length}(\text{private chain}) - \text{length}(\text{public chain})$ 
16   append new block to public chain
17   if  $\Delta_{prev} = 0$  then
18     private chain  $\leftarrow$  public chain
19      $\text{privateBranchLen} \leftarrow 0$ 
20   else if  $\Delta_{prev} = 1$  then
21     publish last block of the private chain
22   else if  $\Delta_{prev} = 2$  then
23     publish all of the private chain
24      $\text{privateBranchLen} \leftarrow 0$ 
25   else
26     publish first unpublished block in private block.
27   Mine at the head of the private chain.
```

(Was tie with branch of 1)
(Pool wins due to the lead of 1)

(they win)

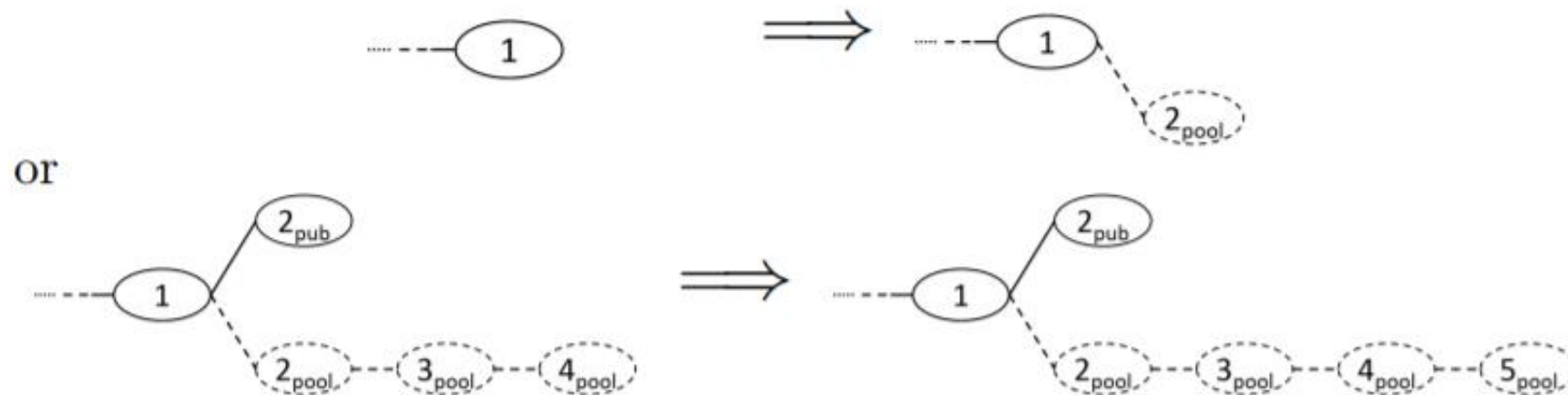
(Now same length. Try our luck)

(Pool wins due to the lead of 1)

($\Delta_{prev} > 2$)

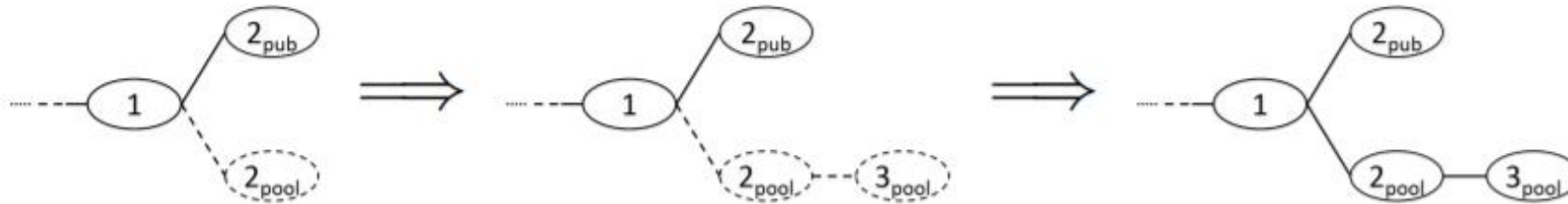
Strategy

- (a) *Any state but two branches of length 1, pools finds a block. The pool appends one block to its private branch, increasing its lead on the public branch by one. The revenue from this block will be determined later.*



Strategy

- (b) *Was two branches of length 1, pools finds a block. The pool publishes its secret branch of length two, thus obtaining a revenue of two.*



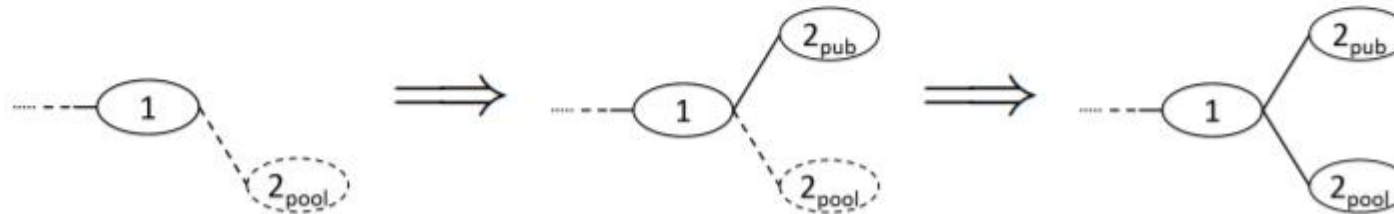
- (c) *Was two branches of length 1, others find a block after pool head. The pool and the others obtain a revenue of one each — the others for the new head, the pool for its predecessor.*



Strategy

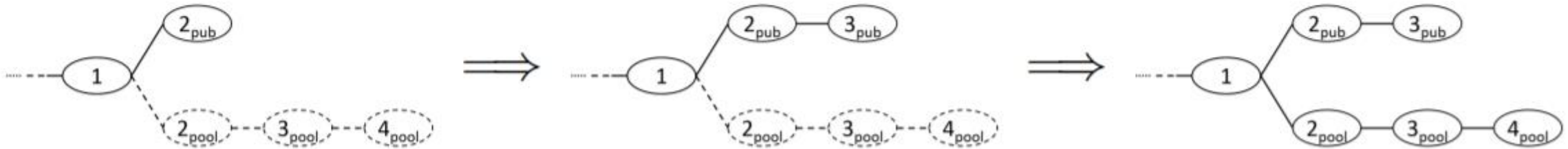
- (f) *Lead was 1, others find a block.* Now there are two branches of length one, and the pool publishes its single secret block. The pool tries to mine on its previously private head, and the others split between the two heads. Denote by γ the ratio of others that choose the non-pool block.

The revenue from this block cannot be determined yet, because it depends on which branch will win. It will be counted later.



Strategy

- (g) *Lead was 2, others find a block.* The others almost close the gap as the lead drops to 1. The pool publishes its secret blocks, causing everybody to start mining at the head of the previously private branch, since it is longer. The pool obtains a revenue of two.



Analysis

- ❖ The states of the system represent the lead of the selfish pool; that is, the difference between the number of unpublished blocks in the pool's private branch and the length of the public branch.

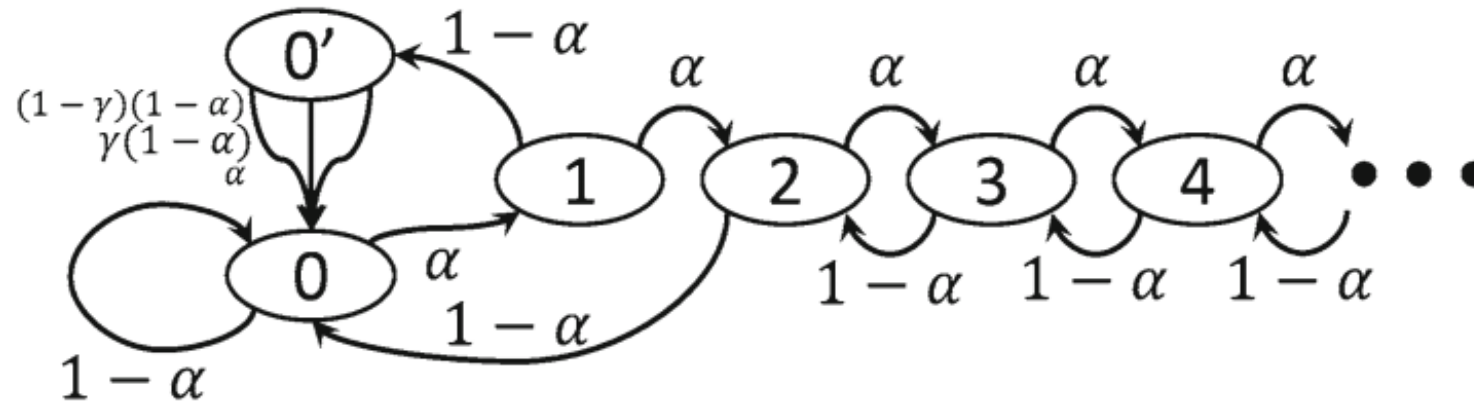


Fig. 1. State machine with transition frequencies.

State Probabilities

$$\begin{cases} \alpha p_0 = (1 - \alpha)p_1 + (1 - \alpha)p_2 \\ p_{0'} = (1 - \alpha)p_1 \\ \alpha p_1 = (1 - \alpha)p_2 \\ \forall k \geq 2 : \alpha p_k = (1 - \alpha)p_{k+1} \\ \sum_{k=0}^{\infty} p_k + p_{0'} = 1 \end{cases}$$

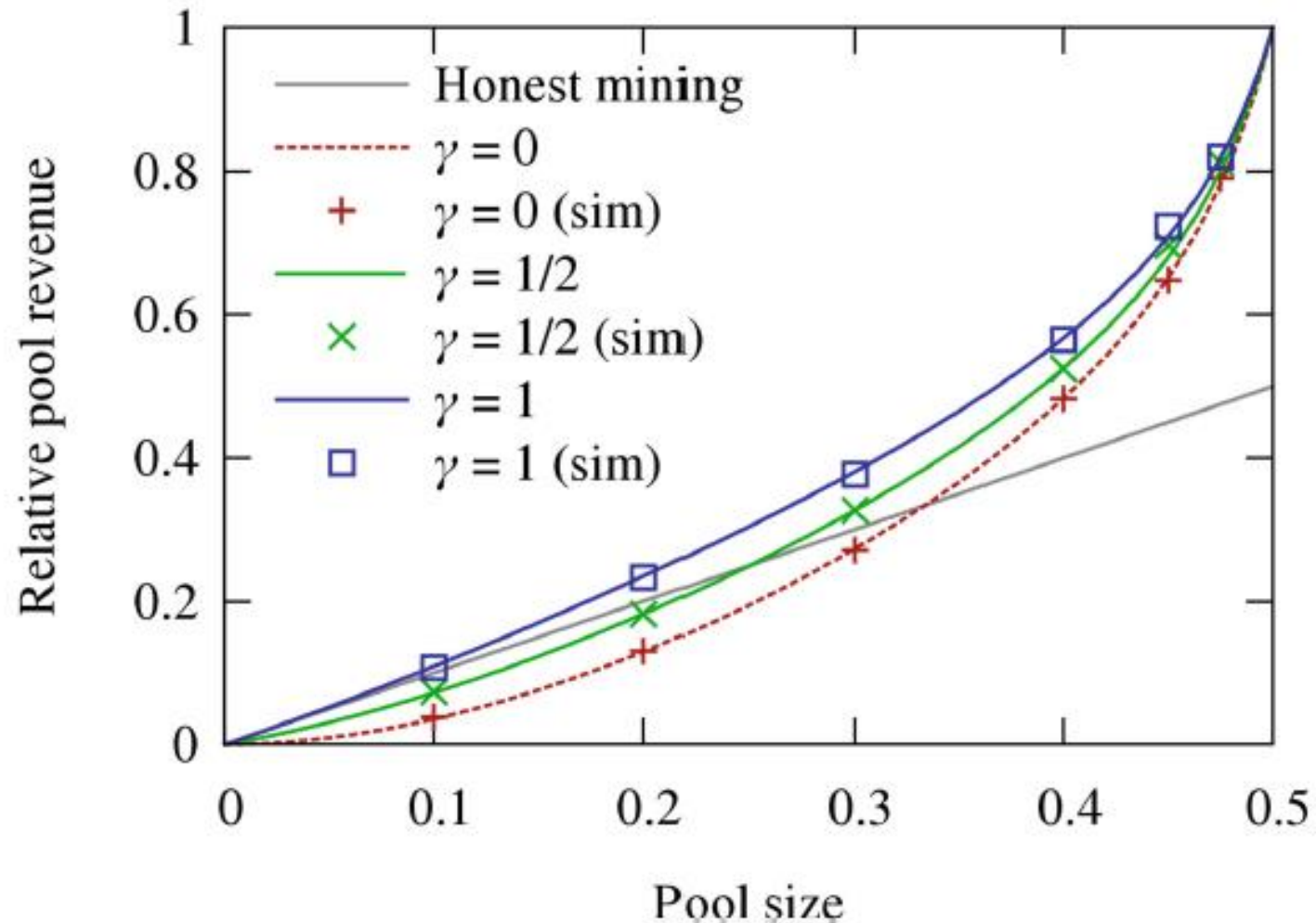
$$p_0 = \frac{\alpha - 2\alpha^2}{\alpha(2\alpha^3 - 4\alpha^2 + 1)}$$

$$p_{0'} = \frac{(1 - \alpha)(\alpha - 2\alpha^2)}{1 - 4\alpha^2 + 2\alpha^3}$$

$$p_1 = \frac{\alpha - 2\alpha^2}{2\alpha^3 - 4\alpha^2 + 1}$$

$$\forall k \geq 2 : p_k = \left(\frac{\alpha}{1 - \alpha} \right)^{k-1} \frac{\alpha - 2\alpha^2}{2\alpha^3 - 4\alpha^2 + 1}$$

Simulation



- ❖ γ : An attacker's network capability
- ❖ When an attacker possesses more than 33% computational power, the attacker can always earn extra rewards.

Observation

Observation 1 *For a given γ , a pool of size α obtains a revenue larger than its relative size for α in the following range:*

$$\frac{1-\gamma}{3-2\gamma} < \alpha < \frac{1}{2} . \quad (9)$$

Observation 2 *For a pool running the Selfish-Mine strategy, the revenue of each pool member increases with pool size for pools larger than the threshold.*

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Observation 2 *For a pool running the Selfish-Mine strategy, the revenue of each pool member increases with pool size for pools larger than the threshold.*

The selfish pool would therefore increase in size, unopposed by any mechanism, *towards a majority.*

Countermeasure

- ❖ When a miner learns of competing branches of the same length, it should propagate all of them, and choose which one to mine on **uniformly at random**.


$$\gamma = \frac{1}{2}, \text{ Threshold} = \frac{1}{4}$$

Selfish Mining



Selfish Mining



Concurrent paper

❖ Theoretical Bitcoin Attacks with less than Half of the Computational Power

The basic block-discarding idea, and a strategy to secretly hold new mined block, were explicitly described in 2010-old thread of Bitcoin technical discussions forum[7] including numerical results of a simplified simulation[8]. Despite the participation of influential Bitcoin developers in this forum discussion, the attack has been long forgotten, probably due to allegedly being impractical. Surprisingly, two researchers of Cornell University have recently and independently published a pre-print paper mathematically analyzing the st_1 strategy, which they call "Selfish Mining"[9].²

²Unfortunately the paper results were misleadingly propagated via the web and media[10], causing disproportionate panic among Bitcoin users.

Impractical

- ❖ The value of γ cannot be 1 because when the intentional fork occurs, the honest miner who generated a block will select his block, not that of the selfish miner.
- ❖ Honest miners can easily detect that their pool manager is a selfish mining attacker.
 - If the manager does not propagate blocks immediately when honest miners generate blocks, the honest miners will know that their pool manager is an attacker.
 - The blockchain has an abnormal shape when a selfish miner exists.

Optimal selfish mining

- ❖ Optimal selfish mining strategies in bitcoin
- ❖ Stubborn mining: Generalizing selfish mining and combining with an eclipse attack
-

Thank You!

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